Electro-mechanical demultiplexer enabled by tunable electric circuits

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\begin{abstract}
Inspired by the electronic demultiplexer, acoustic/elastic demultiplexers have received much attention in recent years. An acoustic/elastic demultiplexer can split one input wave signal into several output wave signals based on their frequencies. However, little to no work has been reported on the acoustic/elastic demultiplexers by considering the electro-mechanical coupling. In this letter, a multi-channel demultiplexer is proposed based on one-dimensional piezoelectric metamaterial plates connecting with shunting circuits. In particular, a four-channel electro-mechanical demultiplexer consisting of three electrically connected plates is constructed. As an outstanding example, the electro-mechanical wave with a certain frequency could propagate along a desired path. The underlying design principle relies on the indisputable character of the bandgaps of the piezoelectric plates, which are highly tunable by the external LC circuits. A numerical simulation is carried out by the two-dimensional spectral element method to validate the feasibility of the four-channel demultiplexer. Similarly to crystal filters or crystal oscillators, the proposed electro-mechanical demultiplexer could be integrated into some electronic devices, which may provide a wide range of applications in wireless telecommunication and electric signal processing.
\end{abstract}

1. Introduction

Phononic crystals and acoustic/elastic metamaterials are artificial materials or structures, whose material properties and/or geometries generally vary periodically in the space. Their outstanding capacity for the control of acoustic/elastic waves has received much research interest \cite{1,2}. Some unprecedented acoustic/elastic wave phenomena or novel acoustic wave devices have been realized based on phononic crystals or acoustic/elastic metamaterials, such as negative refraction \cite{3}, unidirectional propagation \cite{4}, focusing \cite{5}, wave filtering \cite{6}, sensors \cite{7}, waveguides \cite{8}, superlenses \cite{9}, cloaking \cite{10}, etc. Bandgaps are one of the most important properties of such materials, in which the wave propagation is prohibited. The bandgaps induced by Bragg scattering are referred to as the Bragg bandgaps due to the periodic variation of acoustic impedance. The bandgaps generated by local resonances of the unit-cell are called the resonance bandgaps. The bandgaps are often unchangeable in the conventional phononic crystals or acoustic metamaterials after they are designed and manufactured, which may limit their practical applications. To overcome this limitation, some efforts have been made to achieve the tunable bandgaps by making use of the pre-deformation \cite{11,12}, the multi-field coupling \cite{13–15}, etc.

Electronic demultiplexer is a combinational logic circuit or switch, which can split one input signal into several signals outputting from different channels. Inspired by this, the researches on acoustic/elastic demultiplexers have flourished as the development of phononic crystals and acoustic metamaterials in recent years. The acoustic/elastic demultiplexers can split one multi-frequency wave signal into several single-frequency wave signals outputting from different channels, see Fig. 1b. It was proven that the acoustic/elastic waves can be guided into different output channels based on their frequencies by introducing the appropriate line or point defects into a phononic crystal \cite{16–20}. In addition, the parallel connection of phononic crystals with the tunable band structures was also adopted to design the elastic/ acoustic demultiplexers, in which the waves with the specific

\begin{figure}[h]
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\includegraphics[width=\textwidth]{figure1.png}
\caption{Illustration of the acoustic/elastic demultiplexer.}
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\begin{figure}[h]
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\includegraphics[width=\textwidth]{figure2.png}
\caption{Numerical simulation results of the four-channel demultiplexer.}
\end{figure}

\begin{figure}[h]
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\includegraphics[width=\textwidth]{figure3.png}
\caption{Experimental setup of the four-channel demultiplexer.}
\end{figure}
Fig. 1. The schematic illustration of the electro-mechanical demultiplexer. (a) The piezoelectric plate attached symmetrically with an array of periodic electrodes connected by the LC circuits, (b) the conceptual illustration of the 4-channel electro-mechanical demultiplexer made of three electrically connected piezoelectric plates. The three piezoelectric plates (plates I, II, III) are the same except the magnitudes of the inductances and the capacitances, and are connected by the wires. The circuits for the regions P1–P6 are shown in P_A and P_B.

frequencies can only transmit along the target routes [21,22]. To the knowledge of the authors, until now there is no report on elastic/acoustic demultiplexers with the electro-mechanical coupling, which however may further broaden their practical applications. Actually, the acoustic wave devices based on electromagnetic materials have already obtained huge applications in a wide range. For example, crystal filters [23,24] and surface acoustic wave filters [25] were both developed based on piezoelectric materials, which play a particularly important role in the development of narrow-band communication systems and today’s highly complex electronic products. Piezoelectric materials can transform the electric energy into the mechanical energy and vice versa, and their performance is excellent in terms of frequency selectivity and frequency stability.

2. Design of electro-mechanical demultiplexer

2.1. Structure description

In this letter, the concept of electro-mechanical demultiplexer is proposed and realized based on piezoelectric metamaterials. In the proposed demultiplexer, the electro-mechanical waves of different frequencies can transmit along the respective routes and output from the corresponding channels, see Fig. 1b. The designed piezoelectric metamaterials have simple configurations, which are realized by integrating the periodic electrodes onto the surfaces of the homogeneous piezoelectric plates and connecting the top and the bottom electrodes with the external LC circuits, see Fig. 1a. The researches on such kind of piezoelectric phononic crystals or metamaterials indicate that their band structures can be tuned nondestructively by the external circuits [26–33]. Compared with the external circuits containing either the capacitors or the inductors only, the external circuits containing both the capacitors and the inductors (LC circuits) can control the resonance bandgaps of the symmetric Lamb waves propagating in the piezoelectric plates much more precisely, i.e. a resonance bandgap can be located in a specified frequency range by the adjustment of the LC circuits [34], which is an indispensable character of the piezoelectric plates for the present demultiplexer. The multi-channel demultiplexer can be obtained through the electric connection of several plates presented in Fig. 1b. For example, the 4-channel demultiplexer is composed of three piezoelectric plates I, II and III, which are connected by the wires, see Fig. 1b. In this letter, these three piezoelectric plates are supposed to be supported by a frame, which is much stiffer than the piezoelectric plates. And the corresponding support points can be regarded as the fixed points. In this way, the waves can hardly propagate from the piezoelectric plates into the frame, and the energy can only flow from the plate I into the plates II and III in an electric form.

Some regions of the plates connected with the same external LC circuits can be regarded as a finite piezoelectric metamaterial plate, which are labeled as P_A and P_B in Fig. 1a or P1–P6 in Fig. 1b. Each piezoelectric metamaterial plate is composed of n unit cells. The two finite metamaterial plates realized by using the same piezoelectric plate are connected by the input channel naturally, i.e. P1 and P2 for plate I, P3 and P4 for plate II and P5 and P6 for plate III. The distribution of the electrodes on each piezoelectric plate is symmetric with respect to the input channel in the middle. The energy is imported via the input channel and exported via the output channels on the two ends of each piezoelectric plate. The magnitudes of the inductances and the capacitances could be determined based on the analysis of the bandgaps of each metamaterial plate. The present electro-mechanical demultiplexer is a hierarchical structure, and the number of output channels can be increased or decreased by connecting or disconnecting the piezoelectric plates.
As in Ref. [35], the piezoelectric metamaterial plate is assumed to be made of PZ26 polarized along the thickness direction ($x_3$-direction) and covered by very thin periodic electrodes. The material parameters for PZ26 are $\rho = 7700$ kg/m$^3$, $c_{11} = 148$ GPa, $c_{13} = 85$ GPa, $c_{33} = 135$ GPa, $c_{44} = 28$ GPa, $\varepsilon_1 = 9.86$ C/m$^2$, $\varepsilon_{31} = -2.8$ C/m$^2$, $\varepsilon_{33} = 12.5$ C/m$^2$, $\varepsilon_{11} = 800 = 800 \varepsilon_0$, $\varepsilon_{33} = 700 = 700 \varepsilon_0$, where $\varepsilon_0$ is the vacuum permittivity. Thus, the mass and the stiffness of such electrodes are negligible. The unit cells are formed due to the periodic surface electrodes. The widths of the unit cell and the electrode are represented by $w_e$ and $w_r$, respectively. The thickness of the piezoelectric plate is denoted by $h$. The length of the plate in the direction perpendicular to the $x_1 - x_3$ plane is $l$, which is assumed to be much larger than $h$. Thus, the piezoelectric plate is considered to be in the plane-strain state in our numerical simulation.

2.2. Bandgap analysis

The two-dimensional (2D) spectral element method (SEM) for the electro-elastic waves propagating in piezoelectric plates connecting with shunting circuits [34] is adopted to solve the problem under consideration, which is presented in Supplementary Material 1 (see Appendix A). The separate piezoelectric plates are connected by the wires via the electrodes. The two connected electrodes (a and b) have to satisfy the following electric conditions as

$$V_a = V_b, \quad D_a + D_b = 0,$$

where $V_b$, $V_a$, and $D_a$, $D_b$ are the electric potentials and the electric displacements, respectively.

Since the antisymmetric Lamb waves can be generated only by a voltage difference between the top and bottom plate surfaces, there is no coupling between the antisymmetric Lamb waves and the external circuits in our considered case. Thus, we only take the symmetric Lamb waves into account. Our design of the demultiplexer relies on the analysis of the corresponding bandgaps, which are obtained through the dispersion curves for the unit cell imposed by the Bloch–Floquet periodic boundary conditions. The high tunability of the bandgaps is necessary for our design. Therefore, the Bragg bandgaps are inappropriate for our purpose due to their low tenability [34–36], and only the bandgaps in the low-frequency or long-wavelength range [36], $C_r$, has to be determined numerically. In this study, the equivalent capacitance $C_r$ of the whole piezoelectric component is determined directly in a numerical way. Specifically, the dispersion curves can be determined as shown in Fig. 3b when the magnitudes of $L$ and $C$ are given. The points marked by the crosses in Fig. 3b on the dispersion curves for the infinite wavelength ($\tilde{k} \rightarrow 0$) lying above the upper boundaries of the resonance bandgaps are used to approximately evaluate the resonance frequency $\omega_r$. Then, the value of $C_r$ can be backward calculated. For example, $C_r$ is approximately 0.807C and 0.986C for $w_c/w_a = 1/2$ and 7/8, respectively. For convenience, the resonance frequency is normalized as $\tilde{\omega}_r = 1/\sqrt{\tilde{L}\tilde{C}_T}$, where the dimensionless quantities are defined by $\tilde{\omega}_r = \omega_r\omega_a/\sqrt{c_{33}/\rho}$, $\tilde{C}_T = C_T/C_0$, $\tilde{L} = L/L_0$. $C_0 = hw_a\varepsilon_{33}^2/\hbar$, $L_0 = 1/C_0\omega_a^2$, and $\varepsilon_{33}^* = \varepsilon_{33} (1 + \varepsilon_{33}^2/(\varepsilon_{33}\varepsilon_{33}))$ is the equivalent dielectric constant, $\varepsilon_{33}$ and $\varepsilon_{33}^*$ are respectively the electro-elastic coupling coefficient and the dielectric constant, and $\rho$ is the mass density of the plate.

2.3. Adjusting bandgaps by LC circuits

The more flat the dispersion curve lying above the resonance bandgap, the closer the upper boundary of the bandgap to the resonance frequency $\tilde{\omega}_r$ (see Fig. 3b), the more accurate the prediction will be. Thus, the narrower electrodes are selected for the electro-mechanical demultiplexer as $w_c/w_a = 1/2$. The reason to select the LC circuits as the external circuits is that the resonance bandgaps in the low-frequency region can be tuned arbitrarily by the simultaneous adjustment of the inductors and the capacitors [34].

It means that the upper boundary and the width of the resonance bandgap can be tuned independently, see Fig. 3c. Specifically, the upper boundary of the resonance bandgap is adjusted

![Fig. 2. The equivalent circuit. $C_1$ and $C_2$ represent the equivalent capacitances of the part covered by the electrodes and the rest uncovered part, respectively, $C_r = C_1 + C_2$ represents the total equivalent capacitance of the whole piezoelectric component, and $C_1$ represents the total capacitance of the whole circuit (unit cell).](image-url)
Fig. 3. The dispersion curves of the symmetric Lamb wave for the unit cell. (a) The influence of the plate thickness on the dispersion curves. (b) The influence of the electrode length on the dispersion curves. (c) The independent tunability of the bandwidth of the resonance bandgap. The parameters used in each figure are set as (a) \( \frac{w_e}{w_u} = \frac{1}{2}, \ T = 0.125, \ T = 1 \), (b) \( \frac{h}{w_u} = 1, \ L = 0.125, \ C = 1 \), and (c) \( \frac{w_e}{w_u} = \frac{1}{2}, h = w_u \). The shadow areas represent the bandgaps.

Fig. 4. The distributions of the resonance bandgaps for the piezoelectric metamaterial plates P1–P6 for the specified operating frequencies of the electro-mechanical demultiplexer.

to the target position firstly, and it can almost keep unchanged if we fix the resonance frequency \( \omega_r \). Then the bandwidth can be changed via the adjustment of the inductances. In some particular cases, however, the upper boundary may slightly deviate from the original position. In these cases, we need to fix the inductance while let the upper boundary move back to its original position by slightly changing the value of the resonance frequency \( \omega_r \). The target resonance bandgaps can be finally obtained by repeating these steps.

The design of the appropriate resonance bandgaps for the metamaterial plates P1–P6 is the most important step among the whole process. It is intended that the electro-mechanical wave with the specified frequency could transmit along the target path. It means that this wave should attenuate quickly on the other paths. An example is demonstrated to show how to determine the resonance bandgaps for each metamaterial plate when the operating frequencies of the electro-mechanical demultiplexer are chosen. It is assumed that the four operating frequencies are 395.828 kHz, 420.916 kHz, 451.578 kHz and 469.697 kHz, whose normalized values are calculated as \( f_1 = 1.42, f_2 = 1.51, f_3 = 1.62, f_4 = 1.685 \), respectively. And the electro-mechanical waves with the frequencies \( f_1 - f_4 \) are supposed to output from the channels 1–4, respectively. Thus, for the plate I, the resonance bandgaps of P1 and P2 should cover the frequencies \( f_3 \) and \( f_4 \) and the frequencies \( f_1 \) and \( f_2 \), respectively, see the top two figures in Fig. 4. In this way, the waves with the frequencies \( f_1 \) and \( f_2 \) and the waves with the frequencies \( f_3 \) and \( f_4 \) can transmit into the plate II and plate III, separately. Similarly, for plate II, the resonance bandgaps of P3 and P4 should cover the frequencies \( f_2 \) and \( f_1 \), respectively, see the first two figures on the bottom of Fig. 4. And for plate III, the resonance bandgaps of P5 and P6 should cover the frequencies \( f_4 \) and \( f_3 \), respectively, see the last two figures on the bottom of Fig. 4. The magnitudes of the inductances and the capacitances of the LC circuits for the
different metamaterial plates can be figured out when the desired resonance bandgaps are specified.

3. Device simulation

As a verification, a 2D numerical simulation is carried out for the 4-channel electro-mechanical demultiplexer described in Fig. 1b in the frequency domain. Referring to the experimental sample in the Ref. [35], the length and the thickness of the unit cells are both selected as 2 mm and each piezoelectric plate (I–III) is composed of 41 unit cells. Thus, each partial metamaterial plate (P1–P6) contains 19 unit cells. The input cell is fully covered by the electrodes and the rest cells are partly covered by the electrodes and the width of the electrodes is 1 mm, see Fig. 1a. The input signal is a voltage ($V_1 = 200$ V), which is applied on the top electrode in the middle of plate I. And the corresponding bottom electrode is grounded. The voltages are applied at the four different frequencies $f_1$ – $f_4$, respectively. It should be pointed out that the symmetric boundary supports have practically no influences on the bandgaps of the symmetric Lamb waves. The distribution of the logarithm of the displacement field $G = 20 \log_{10} u$ in the 4-channel electro-mechanical demultiplexer is plotted in Fig. 5a for the four specified frequencies. It shows clearly that the waves with the different frequencies transmit along the different paths and finally output from the different channels. In Fig. 5b, the variations of the output voltages with the normalized frequency for the different channels are presented. The output voltage is normalized by the input voltage as $G = 20 \log_{10} (V_o / V_I)$. The bandgaps for the different output channels shown in Fig. 5b agree well with the corresponding bandgaps in Fig. 4, which justifies the validity of the present numerical calculations. In addition, Fig. 5b shows that the waves can propagate along the target paths while attenuate quickly along the other paths. It is shown that the voltage at the specified frequency output from each target channel is much higher than the voltages at the other frequencies in the same channel by 100 dB approximately. Thus, we can conclude that the effect of the crosstalk between the different outputs is very small and negligible for the proposed electro-mechanical demultiplexer.

4. Conclusions

In summary, the first electro-mechanical demultiplexer is proposed and realized in this letter based on the novel piezoelectric metamaterial plate in a simple configuration. The independent tunabilities of the upper boundary and the bandwidth of the corresponding resonance bandgaps are indispensable for our design. The feasibility of the 4-channel electro-mechanical demultiplexer is confirmed by a numerical simulation. The present electro-mechanical demultiplexer has the following four outstanding characteristics:

- **The simple structure:** The whole model is only composed of several homogeneous piezoelectric plates. The piezoelectric metamaterial plate is covered by an array of periodic electrodes connected by the external LC circuits, and the different piezoelectric plates are connected electrically.
- **The high tunability:** The working frequencies can be changed at will and nondestructively via the adjustment of the external LC circuits. The number of the output channels can be easily increased or decreased by connecting or disconnecting the piezoelectric plates.
- **The excellent working performance:** The electro-mechanical waves with different frequencies can be split efficiently and the effect of the crosstalk between the different outputs is very small.
- **The electro-mechanical coupling:** The electro-mechanical demultiplexer has the potential to be integrated into some electrical devices just like crystal filters, which may promote the application of the acoustic/elastic demultiplexer in a wide range, such as wireless telecommunication and electric signal processing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.eml.2022.101610.